C:\Documents and Settings\Amy Shaw\Local Settings\Temporary Internet Files\Content.IE5\Y7YD832X\MC900154518[1].wmf **Revision Examination Assessment Papers (REAP)**

**Semester 1 Examination 2012**

**Question/Answer Booklet**

(This paper is not to be released to take home before 25/6/2012)

**MATHEMATICS 3C**

**Section Two:**

**Calculator-assumed**

Name of Student: \_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_ \_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_

**Time allowed for this section**

Reading time before commencing work: 10 minutes

Working time for this section: 100 minutes

**Materials required/recommended for this section**

***To be provided by the supervisor***

This Question/Answer Booklet

Formula Sheet (retained from Section One)

***To be provided by the student***

Standard items: pens, pencils, pencil sharpener, eraser, correction fluid/tape, ruler,

highlighters

Special items: drawing instruments, templates, notes on two unfolded sheets of A4 paper,

and up to three calculators satisfying the conditions set by the Curriculum

Council for this examination

**Important note to students**

No other items may be used in this section of the examination. It is **your** responsibility to ensure

that you do not have any unauthorised notes or other items in the examination room. If you have any unauthorised material with you, hand it to the supervisor **before** reading any further.

**Structure of this paper**

|  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- |
| Section | Number of questions available | Number of questions to be answered | Working time  (minutes) | Marks available | Percentage of exam |
| Section One  Calculator-free | 6 | 6 | 50 | 50 |  |
| Section Two  Calculator-assumed | 12 | 12 | 100 | 100 |  |

|  |  |  |
| --- | --- | --- |
| Total | 150 | 100 |

**Instructions to students**

1 Write your answers in the spaces provided in this Question/Answer Booklet. Spare pages are included at the end of this booklet. They can be used for planning your responses and/or as additional space if required to continue an answer. If you need to use the space to continue an answer, indicate in the original answer space where the answer is continued. i.e. give the page number. Fill in the number of the question(s) that you are continuing to answer at the top of the page.

2 **Show all your working clearly**. Your working should be in sufficient detail to allow your answers to be checked readily and for marks to be awarded for reasoning. Incorrect answers given without supporting reasoning cannot be allocated any marks. For any question or part question worth more than two marks, valid working or justification is required to receive full marks. If you repeat an answer to any question, ensure that you cancel the answer you do not wish to have marked.

3 It is recommended that you **do not use pencil**, except in diagrams.

**Section Two: Calculator-assumed (100 marks)**

This section has **twelve (12)** questions. Answer all questions. Write your answers in the spaces provided.

Working time: 100 minutes

\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_

**Question 7 (10 marks)**

(a) Emily is a very strong soccer player who has a probability of  of scoring a goal with each attempt. She has 15 attempts. Find the probability that the number of goals she scores is less than 7. (2)

(b) Suppose that Y is distributed normally with unknown mean  and standard deviation .

Given that , find the value of . (2)

(c) Alice, Bronwyn and Cathy independently each think of an integer in the set { 1,2,3,4,5,6,7 }

Find the **probability** that, of the three integers selected,

1. all three are greater than 4 (1)

**Question 7 (continued)**

(c) (ii) all three are greater than 5 (1)

(iii) the least integer is 5. (1)

(iv) the three integers are different given that the least integer selected is 5. (2)

(v) the sum of the three integers is more than 15. (1)

**Question 8 (7 marks)**

(a) It takes 12 hours to drain a storage tank by opening the valve at the bottom. The depth *‘y*’ of fluid in the tank *‘t’* hours after the valve is opened is given by metres.

1. Find the rate  m/hour at which the tank is draining at time, *t*. (2)
2. When is the fluid in the tank falling fastest and slowest?

What are the values of  at these times? (2)

**Question 8 (continued)**

(b) If the volume of a cylinder is given by , find the appropriate percentage change in *V* when *r* changes by % (3)

**Question 9 (10 marks)**

|  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- |
| *x* | 3 | 1 | 2 | 3 | 5 | 0 |
| P(X=*x*) | 0.0 | 0.1 | 0.4 | 0.1 | 0.2 | 0.3 |

(a) Give two reasons why the following cannot be a probability distribution. (2)

(b) The probability distribution of *x* where random variable, X is the sum of the uppermost numbers when two fair die are rolled is tabulated below.

|  |  |  |  |  |  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- |
| *x* | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 |
| P(X=*x*) |  |  |  |  |  |  |  |  |  |  |  |

Find

1.  (2)
2.  (2)
3. If event A is  and event B is, are these two events independent? Justify your answer. (4)

**Question 10 (7 marks)**

(a) The function *f(x)* is differentiable for all  and satisfies the conditions

*f’(x)* < 0 where *x < 2*

*f’(x) =* 0 where *x = 2*

*f’(x )=* 0 where *x = 4*

*f’(x) >* 0 where *2 < x < 4*

*f’(x) >* 0 where *x > 4*

1. Draw a sketch of this function *f(x).*  (3)



1. State whether the following statement is true or false.

“The graph *f(x)* has a stationary point of inflection where *x=4”.*  (1)

(b) If , find  (3)

**Question 11 (7 marks)**

(a) The function  is transformed to .

Describe the transformation in order. (3)

(b) The curve C has equation  and is drawn below



.

A(1, 0.37)

1. Sketch the graph of . (2)



**Question 11 (continued)**

1. State the coordinates of A if the curve is transformed to  (2)

**Question 12 (9 marks)**

(a) A company produces fruit balls coated in either dark chocolate or milk chocolate. A large number of these fruit balls are placed in a box. Twenty per cent of the fruit balls in the box are coated with dark chocolate.

1. Calculate  (1)
2. A random sample of ten fruit balls is taken from the box.

Explain the meaning of  with respect to this sample. (2)

(b) (i) Find *n* given that =0.167 772 16 (1)

(ii) Explain the meaning of your answer to part (b) with respect to the fruit balls. (2)

**Question 12 (continued)**

(c) The curve  and  intersect at the point (0, 1) as shown in the diagram.



Find the area enclosed by the curves and the line *x=2.*

Leave your answer in terms of ‘*e*’. (3)

**Question 13 (8 marks)**

Adam paints garden gnomes to sell. He sends the garden gnomes to his father (a qualified quality controller) in the order of completion, who classifies them as either ‘Superior’ or ‘Regular’, depending on the quality of their finish.

If the garden gnome is Superior, then the probability that the next garden gnome is superior is 0.9. If the garden gnome is Regular, then the probability that the next garden gnome is superior is 0.7.

(a) If the first garden gnome inspected is Superior, find the probability that the third gnome

is Regular. (2)

(b) If the first garden gnome inspected is Superior, find the probability that the next three

gnomes are Superior. (1)

(c) A group of 3 consecutive garden gnomes is inspected and the first is a Regular. It is also

found that of these three gnomes,

P(no Superior) = 0.09

P( 1 Superior) = 0.28

P( 2 Superior) = 0.63

Find the expected number of these gnomes that will be Superior. (2)

**Question 13 (continued)**

(d) Adam’s little brother, Brodie joins in this business venture. The probability that any one of

Brodie’s painted garden gnomes is Regular is 0.8. He wants to ensure that the probability that he paints at least two Superior is at least 0.9. Calculate the minimum number of garden

gnomes that Brodie would need to paint to achieve this aim. (3)

**Question 14 (9 marks)**

A piece of wire 8cm long is cut into two unequal parts. One part is used to form a rectangle that has a length three times its width. The other part of the wire is used to form a square.

(i) If the width of the rectangle is *x* units, determine an equation that will give

the sum of the areas of the rectangle and the square in terms of *x*. (4)

(ii) Using Calculus, find the length of each part of the wire when the sum of the areas is a minimum. (5)

**Question 15 (11 marks)**

Nuts and Bolts Company manufactures 120mm bolts which are normally distributed with a mean length of 120mm and a standard deviation of 1mm. Only bolts which are between 118.6mm and 121.4mm pass inspection and are packaged as 120mm bolts.

(a) Find the probability of a randomly selected bolt being an acceptable length. (2)

(b) Find the expected number of acceptable bolts in a batch of 100 000 (1)

(c) Is this a reasonable outcome for the company? Justify your answer. (2)

(d) A new quality controller suggests adjusting the settings on the machines so that the

standard deviation becomes 0.85mm and that only the shortest 5% and the longest 5% of the bolts are rejected.

1. Find the new minimum and maximum acceptable lengths

correct to the nearest 0.1mm. (3)

1. Do the packages contain bolts that are more consistent in length? (1)
2. Is the manufacturer better off? Justify. (2)

**Question 16 (7 marks)**

The graph of g’(x) is given below.



(a) What can be said about the gradient of the function g(x) between x =-3 to x= 1? (1)

(b) When does the function, g(x) have a negative gradient? (1)

(c) State an equation for the tangent to the graph of g(x) at x = 3. (2)

(d) Find the value of *x* at which  has a relative maximum for  (1)

(e) Find the *x*-coordinate of each point of inflection of the graph of for  (2)

**Question 17 (9 marks)**

(a) Shade the region, R, bounded by the curves,, , and  in the diagram.

Find the area of the region R, showing all working steps. (4)



**Question 17 (continued)**

(b) A group of anthropologists found that human tooth size is continuing to decrease, such that



In Northern Europeans, for example, tooth size reduction now has a rate of 1% per 1000 years.

1. If ***t*** represents time in years and ***S*** represents tooth size, find the value of **k**.

(2)

1. In how many years will human tooth size be 90% of their present size? (2)
2. What will be our descendant’s tooth size 20 000 years from now? (1)

(as a percentage of our present tooth size)

**Question 18 (6 marks)**

(a) For the function  below



It is known that

,



The area under the curve from  to  is 80 square units.

Use the information above and mathematical reasoning to determine the value of each of the following.

(i)  (2)

(ii) the area between the curve and the x-axis from  to  (1)

**Question 18 (continued)**

(iii)  (1)

(b) The graph of a function consists of a semi- circle and two line segments as shown.

Find the exact value of  (2)

